

# Thermal Expansivity

## A. Underpinning Purposes

1. Experience in using a *known* substance to calibrate a device, for subsequent application to an *unknown* substance.
2. Acquaintance with two simple devices — the *pycnometer* and the *dilatometer* — capable of giving very precise results for a fundamental physical property of liquid substances.

## B. Theory

1.  $\alpha \equiv \frac{1}{V} \left( \frac{\partial V}{\partial T} \right)_P = \left( \frac{\partial \ln V}{\partial T} \right)_P$  and, since  $\rho = m/V$ ,  $\alpha = - \left( \frac{\partial \ln \rho}{\partial T} \right)_P$
2. Integration  $\Rightarrow V = V_r \exp[\alpha(T - T_r)]$  where  $\alpha$  is assumed to be independent of  $T$  near some reference  $T = T_r$ .
3. More general: If  $f(T, T_r)$  is a function that = 0 when  $T = T_r$ , where  $V = V_r$ , then if  $V$  is expressed  $V = V_r \exp[f(T, T_r)]$

$$\alpha = df/dT$$

## C. Experiment

1. Known is “standard mean ocean water.” Its density is a function of  $T$ , so calibration requires measuring  $m$  and  $T$ .
2. Both this and the unknown (an alcohol) must be degassed beforehand to prevent air bubble formation.
3. Thermal equilibrium is *not* achieved instantly!
4. Data obtained in range 10-40°C; suffices to determine whether  $\alpha$  is  $T$ -dependent over this range.
5. Etched scales on both devices are in cm and mm.
6. Minor complications:
  - Buoyancy correction in pycnometry masses.
  - Thermal expansivity of Pyrex not negligible.
7. Modified instructions:
  - (1) Do dilatometry for just three  $T$  ranges:  $\sim 15, 25, 35^\circ\text{C}$
  - (2) Get density (pycnometry) for at least 4  $T$ s in this range.