

**Pledge and signature:**

**Note:** If you want your paper returned folded (*i.e.*, score concealed), please print your name on the back.

- (2) A pycnometer is fitted with a capillary extension (like those in our laboratory) having an internal diameter of 1.00 mm. In the initial calibration with water, the capillary height is 17.7 mm above the zero level. Calculate the volume of water ( $\text{cm}^3$ ) in the capillary.

$$0.0139 \text{ cm}^3$$

- (6) The apparent mass of the empty pycnometer and capillary extension is 22.379 g. Filled with water to capillary height 17.7 mm (as above), the apparent mass is 47.912 g. At the temperature of these measurements, the density of water is  $0.998011 \text{ g/cm}^3$ . The density of air may be taken as  $1.19 \text{ mg/mL}$ . Calculate the volume  $V_0$  (*i.e.*, to the zero mark) (a) neglecting the buoyancy of air, and (b) taking it into account.

$$(a) \quad m_{\text{app}} = 25.533 \text{ g} \quad V_{\text{app}} = 25.584 \text{ mL} \quad V_{0,\text{app}} = 25.570 \text{ mL}$$

$$(b) \quad m_{\text{air}} = 0.0304 \text{ g} \quad m = 25.563 \text{ g} \quad V = 25.614 \text{ mL} \quad V_0 = 25.600 \text{ mL}$$

- (4) An unknown liquid is placed in this pycnometer, giving a capillary reading of 17.7 mm when the system is equilibrated at  $27.43^\circ\text{C}$ . When it is reequilibrated at  $29.12^\circ\text{C}$ , the capillary level is 47.1 mm. (a) Calculate the average  $\alpha$  for this liquid over this temperature range. (b) What would be the best temperature to record for this estimate of  $\alpha$ ?

$$(a) \quad V = h \cdot r^2 = 0.02309 \text{ mL}$$

$$= 1/V \left( \frac{V}{T} \right)_P \quad \frac{V}{T} = \frac{0.02309}{25.6 \text{ (1.69 K)}} = 5.34 \times 10^{-4} \text{ K}^{-1}$$

$$(b) \quad 28.28^\circ\text{C}$$

- (3) If each of the capillary measurements in (3) above is uncertain by 0.3 mm, and if this is the only significant source of uncertainty, what is the % uncertainty in the estimated value of  $\alpha$ ?

$$s_h = (0.3^2 + 0.3^2)^{1/2} = 0.42 \text{ mm} \quad \text{rel. err in } h = 0.42/29.4 = 1.4\%$$

- (1) If the density of a fluid is represented as  $\rho = \rho_0 \exp(bx + cx^2)$ , where  $x = t(^{\circ}\text{C}) - 25^\circ\text{C}$ , what is the physical meaning of  $\rho_0$ ?

$$\rho_0 \text{ is the value of } \rho \text{ when } x = 0, \text{ i.e. } t = 25^\circ\text{C}.$$