

Pledge and signature:**Note:** If you want your paper returned folded (i.e., score concealed), please print your name on the back.

1. (7) Consider the probability distribution, $P(x) = c x^2$, defined over the range $-1 \leq x \leq 2$. For this distribution, calculate: (a) the normalization constant, (b) the mean, (c) the variance, and (d) the standard deviation.

(a) $1/3$ (b) $5/4$ (c) $11/5 - (5/4)^2 = 51/80$ (d) $(51/80)^{1/2}$
2. (6) (a) If you generate 10^6 random numbers having this distribution, how many are expected to fall within the x range 1.40–1.50? And what is the standard deviation of this value?
 (b) If you now generate 10^6 such random numbers, what do you get in place of your results in 2a?
 (c) Compare the *per cent* standard deviations in a and b.
 (a) 7011 and $(7011)^{1/2}$ (b) 70111 and $(70111)^{1/2}$ (c) 1.19% & 0.38%
3. (5) A quantity x is uncertain by 3.0% and y is uncertain by 4.0%. Give the % uncertainties for z in each of the following cases:

a. $z = 9/y$ 4 % d. $z = 5 x/y^2$ $(73)^{1/2}$ %
 b. $z = 3 x^4$ 12 %
 c. $z = 1/\sqrt{8x}$ 1.5 % e. $z = 23 y^2/x$ $(73)^{1/2}$ %
4. (9) **Least Squares and KaleidaGraph.**

(a) The declining exponential function with a background is a very commonly occurring functional form in the analysis of kinetics data. Write **exactly** what you should enter in the KG Define Fit box to fit your kinetics data to this relation

$a \cdot \exp(-b \cdot x) + c$; $a = (\text{nonzero value})$; $b = (\text{same})$; $c = (\text{same})$

(b) Why are bad initial values likely to give you more problems here than in, say, fitting calibration data to a quadratic polynomial?

This is a truly **nonlinear** fit, whereas the polynomial fit is algebraically linear (hence guaranteed to converge for any acceptable starting values).

(c) In one of your KG exercises, you generated 10^4 sums of 12 random numbers. Describe the shape of the resulting histogram, and give the expected mean and standard deviation.

Very nearly Gaussian, mean 6, st. dev. 1. [mean and st. dev. for $\text{sum} = 12 \cdot (\text{values for avg} = 1/2 \text{ and } 1/12).$]

(d) Suppose instead you generated 10^4 sums of 16 random numbers. How would the results change? (Be quantitative.)

Gaussian, mean 8, st. dev. $= 2/3^{1/2}$ [again, both $= 16 \cdot (\text{values for avg} = 1/2 \text{ and } 1/(4 \sqrt{12}))$].]