

Lab Day

Pledge and signature:

Note: If you want your paper returned folded (*i.e.*, score concealed), please print your name on the back.

1. (7) Consider the probability distribution, $P(x) = c x^2$, defined over the range $-1 \leq x \leq 2$. For this distribution, calculate: (a) the normalization constant, (b) the mean, (c) the variance, and (d) the standard deviation.
2. (6) (a) If you generate 10^6 random numbers having this distribution, how many are expected to fall within the x range 1.40–1.50? And what is the standard deviation of this value?

(b) If you now generate 10^6 such random numbers, what do you get in place of your results in 2a?

(c) Compare the *per cent* standard deviations in a and b.

3. (5) A quantity x is uncertain by 3.0% and y is uncertain by 4.0%. Give the % uncertainties for z in each of the following cases:

a. $z = 9/y$

d. $z = 5 x/y^2$

b. $z = 3 x^4$

c. $z = 1/\sqrt{8x}$

e. $z = 23 y^2/x$

4. (9) **Least Squares and KaleidaGraph.**

(a) The declining exponential function with a background is a very commonly occurring functional form in the analysis of kinetics data. Write **exactly** what you should enter in the **KG Define Fit** box to fit your kinetics data to this relation

(b) Why are bad initial values likely to give you more problems here than in, say, fitting calibration data to a quadratic polynomial?

(c) In one of your KG exercises, you generated 10^4 sums of 12 random numbers. Describe the shape of the resulting histogram, and give the expected mean and standard deviation.

(d) Suppose instead you generated 10^4 sums of 16 random numbers. How would the results change? (Be quantitative.)